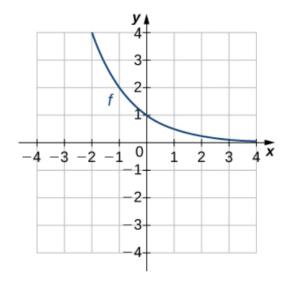
Exercise 196

For the following exercises, use the graph of f to sketch the graph of its inverse function.



Solution

The function graphed in the figure is

$$f(x) = 2^{-x}.$$

To find the inverse function, replace x with y and replace f(x) with x.

$$x = 2^{-y}$$

Solve for y.

$$\ln x = \ln 2^{-y}$$

$$\ln x = -y \ln 2$$

$$y = -\frac{\ln x}{\ln 2}$$

Both functions are plotted together versus x below. Notice that they are reflections of each other across the line y=x.

