## Exercise 196

For the following exercises, use the graph of $f$ to sketch the graph of its inverse function.


## Solution

The function graphed in the figure is

$$
f(x)=2^{-x}
$$

To find the inverse function, replace $x$ with $y$ and replace $f(x)$ with $x$.

$$
x=2^{-y}
$$

Solve for $y$.

$$
\begin{aligned}
\ln x & =\ln 2^{-y} \\
\ln x & =-y \ln 2 \\
y & =-\frac{\ln x}{\ln 2}
\end{aligned}
$$

Both functions are plotted together versus $x$ below. Notice that they are reflections of each other across the line $y=x$.


